## **Abstract**

We study some basic analytical problems for nonlinear Dirac equations involving critical Sobolev exponents on compact spin manifolds. Via variational methods and blow-up analysis, our main target is to study the existence issue of a conformally invariant spinor field equation, which has a strong relationship with Spinorial Weierstraß representation.